

1) Given:

Bat
 $m_B = 2.0 \text{ g}$
 $V_{Bi} = 2.0 \text{ m/s forward}$
 $V_{Bf} = ?$

Insect
 $m_I = .20 \text{ g}$
 $V_{Ii} = 8.0 \text{ m/s backward}$
 $V_{If} = ?$

$$V_{Bf} = V_{If} \Rightarrow V_f$$

Find: ΔKE lost

Soln: Need V_f 1st inelastic eqn

$$\textcircled{1} m_B V_{Bi} + m_I V_{Ii} = V_f (m_B + m_I)$$

$$V_f = \frac{m_B V_{Bi} + m_I V_{Ii}}{m_B + m_I} = \frac{(2.0 \text{ g})(2.0 \text{ m/s}) + (.20 \text{ g})(-8.0 \text{ m/s})}{2.0 \text{ g} + .20 \text{ g}}$$

$$V_f = 1.1 \text{ m/s forward}$$

$$\textcircled{2} KE_i = \frac{1}{2} m_B V_{Bi}^2 + \frac{1}{2} m_I V_{Ii}^2 \quad \text{Note: mass must be in Kg!}$$

$$= \frac{1}{2} (2.0 \times 10^{-3} \text{ kg})(2.0 \text{ m/s})^2 + \frac{1}{2} (2.0 \times 10^{-4} \text{ kg})(-8.0 \text{ m/s})^2$$

$$= 1.0 \times 10^{-2} \text{ J}$$

$$\textcircled{3} KE_f = \frac{1}{2} m_B V_f^2 + \frac{1}{2} m_I V_f^2$$

$$= \frac{1}{2} (2.0 \times 10^{-3} \text{ kg})(1.1 \text{ m/s})^2 + \frac{1}{2} (2.0 \times 10^{-4} \text{ kg})(1.1 \text{ m/s})^2$$

$$KE_f = 1.3 \times 10^{-3} \text{ J}$$

$$\textcircled{4} \Delta KE = KE_f - KE_i = 1.3 \times 10^{-3} \text{ J} - 1.0 \times 10^{-2} \text{ J}$$

$$\Delta KE = -8.7 \times 10^{-3} \text{ J}$$

$$\text{fraction KE Dissipated} = \frac{\Delta KE}{KE_i} = \frac{-8.7 \times 10^{-3} \text{ J}}{1.0 \times 10^{-2} \text{ J}} = \boxed{.87}$$

2) Given:

lion

Boat

$$m_L = 313 \text{ Kg}$$

$$m_B = ?$$

$$V_{Li} = 6.00 \text{ m/s AWAY}$$

$$V_{Bi} = 0$$

$$V_{Lf} = 2.50 \text{ m/s AWAY}$$

$$V_{Bf} = 2.50 \text{ m/s AWAY}$$

$$V_{Lf} = V_{Bf} \Rightarrow V_f$$

Find KE lost in inelastic eqn

Soln: Need mass of Boat 1st

$$\textcircled{1} m_L V_{Li} + m_B V_{Bi} = V_f (m_L + m_B)$$

$$m_L V_{Li} = V_f m_L + V_f m_B$$

$$m_B = \frac{m_L V_{Li} - V_f m_L}{V_f} = \frac{(313 \text{ Kg})(6.00 \text{ m/s}) - (313 \text{ Kg})(2.50 \text{ m/s})}{2.50 \text{ m/s}}$$

$$m_B = 438 \text{ Kg}$$

$$\Delta KE = KE_f - KE_i$$

$$\textcircled{2} KE_i = \frac{1}{2} m_L V_i^2 + \frac{1}{2} m_B V_i^2 = \frac{1}{2} (313 \text{ Kg})(6.00 \text{ m/s})^2$$

$$KE_i = 5630 \text{ J}$$

$$\textcircled{3} KE_f = \frac{1}{2} m_L V_f^2 + \frac{1}{2} m_B V_f^2 = \frac{1}{2} (313 \text{ Kg})(2.50 \text{ m/s})^2 + \frac{1}{2} (438 \text{ Kg})(2.50 \text{ m/s})^2$$

$$KE_f = 2350 \text{ J}$$

$$\Delta KE = KE_f - KE_i = 2350 \text{ J} - 5630 \text{ J}$$

$$\boxed{\Delta KE = -3280 \text{ J}}$$